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# Thermal stress issues in thin film coatings of x-ray optics

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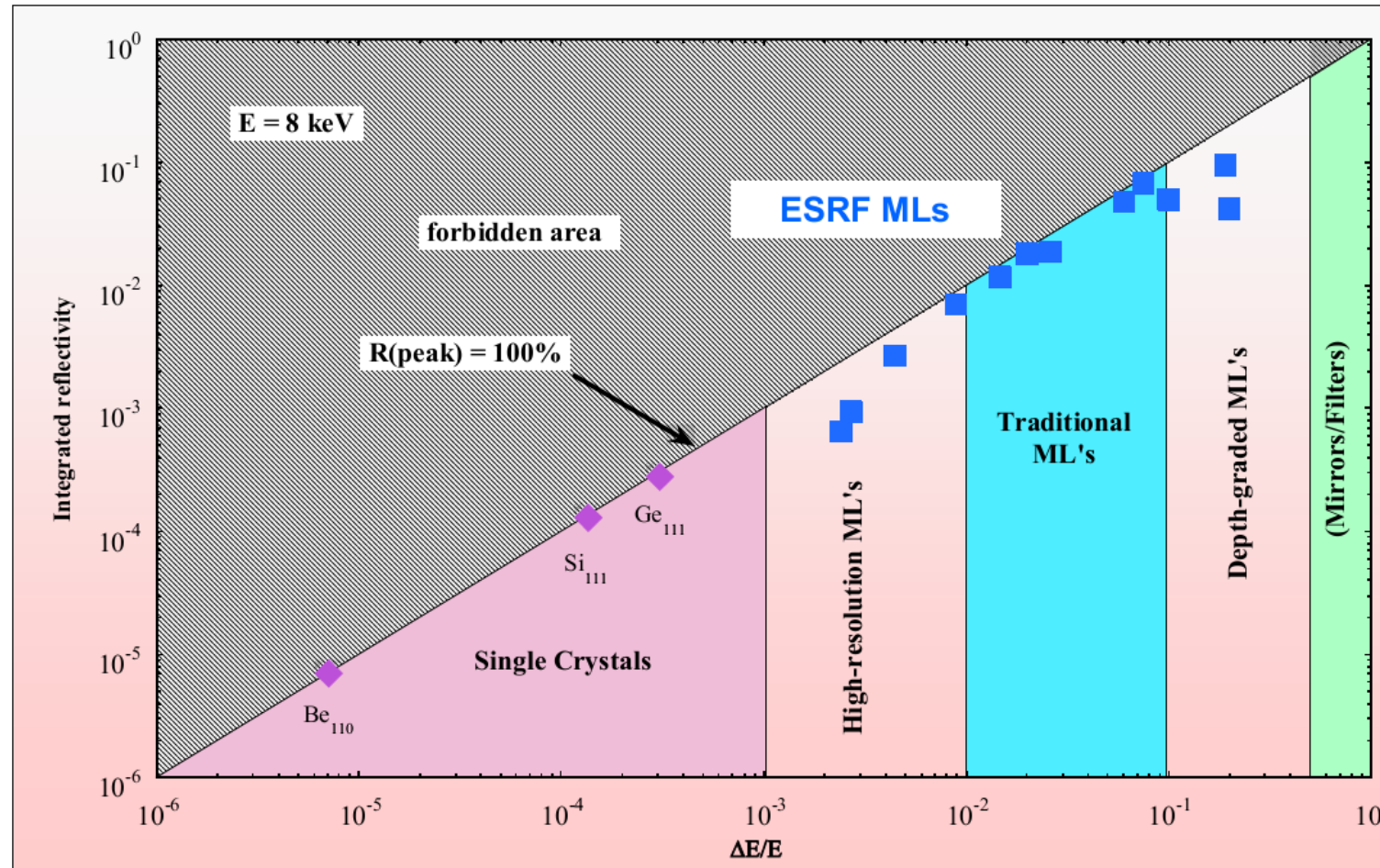
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**Xianchao CHENG**, “*Thermal stress issues in thin film coatings of X-ray optics under high heat load*”,  
**PhD Thesis**, Université de Grenoble, France, 2014

- Introduction
- FE modeling of multilayer optics
- Thermal stress prediction in mirror and multilayer coatings
- Measurement: thermal deformation properties of thin coating film
- Summary and outlook



## Integrated reflectivity versus energy resolution



**Monochromator crystal**

**Multilayer optics**

**Mirror**

# Introduction – Multilayer X-ray optics

- Multilayer structure with two types of alternative sub-layers (very thin) on a substrate. Period:  $\Lambda$

- Multiple Bragg reflections

$$\Lambda = \frac{\lambda}{2\sqrt{n^2 - \cos^2 \theta}} \quad \sim \text{nm}$$

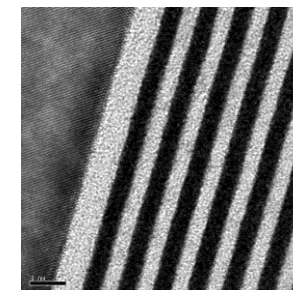
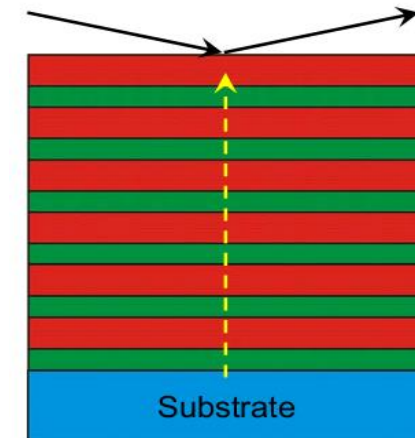
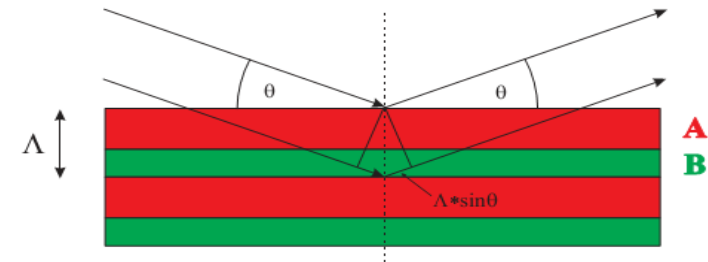
- Situated between Mirror and Monochromator for both photon flux and energy resolution

- Attractive alternative to crystals:

- High photon flux
- Moderate energy resolution
- Harmonics suppression
- Reflectivity enhancement

- Applications

- EUV lithography ( $e_{\text{ph}}=94 \text{ eV}$ )
- “Water window” ( $e_{\text{ph}}=280\ldots 550 \text{ eV}$ )
- Hard x-rays ( $e_{\text{ph}}=1\ldots 100 \text{ keV}$ )



TEM photograph of a Ru/B<sub>4</sub>C multilayer stack

## Thermal deformation

### ➤ First mirror substrate

- Top side water cooling, full length illumination, optimized notches

### ➤ Monochromator crystal

- Liquid nitrogen cooled Silicon crystal
- Water cooled Diamond crystal

## Multilayer optics (with large number of periods of thin coating) :

### ➤ Thermal stress within the layers

### ➤ Thermal deformation

- Substrate + multiple thin layers
- Mutual influences between the substrate and multiple thin layers ?

### ➤ Cooling

- Water or Liquid nitrogen ?

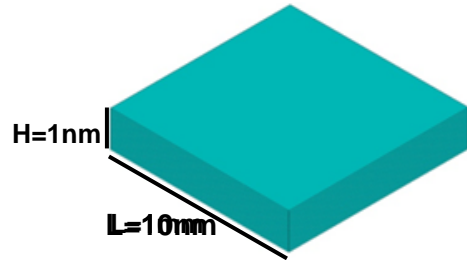
## → FEA + Experiments

# Finite Element Modeling of multilayer optics

## Difficulties of modelling

- High element shape aspect ratio:  $L/H=10^6$   
Program warning happened at  $L/H>20$

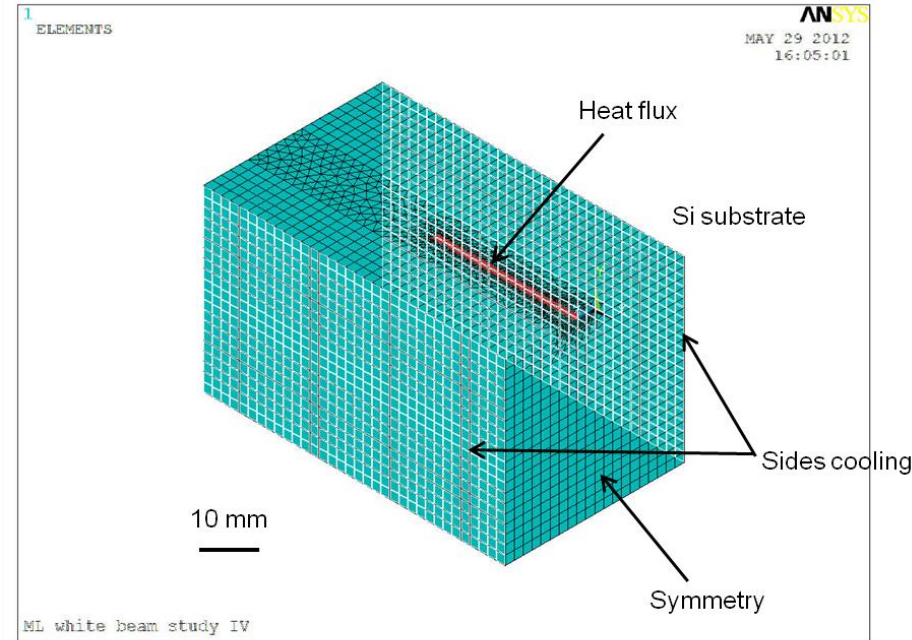
➔ Low solution accuracy



Element geometry, with H zoomed for clarity

- Huge number of elements  
(e.g. with element size  $1 \times 10 \times 10 \text{ nm}^3$ , more than  $5 \times 10^{15}$  elements just for the layer part)

➔ Impossible task for the present computers



Example FE model for substrate

### **The multilayer on top**

- Two types of alternate materials
- Hundreds of layers
- Layer thickness several nanometers

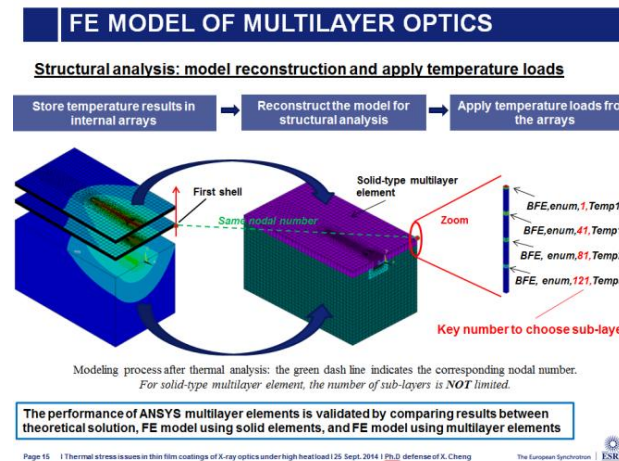
**Very high aspect ratio between the size of the optics and the layer thickness!**



# Finite Element Modeling of multilayer optics

- **ANSYS multilayer elements recently developed (release 12.0 and after, since 2011) for composite materials :**
  - One geometrical Shell element, multiple sub-layers (material properties, temperature or displacement)
  - Thermal analysis: **shell131** (up to 31 sub-layers)
  - Structural analysis, **shell181**, **solsh190**
  - The thermal and structural multilayer elements are not exactly corresponded
  - Structural model needs to be reconstructed, and temperature loading to be applied by use of array parameters
  - Various validation tests performed

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## Mirror

1. Water cooling
2. LN cooling

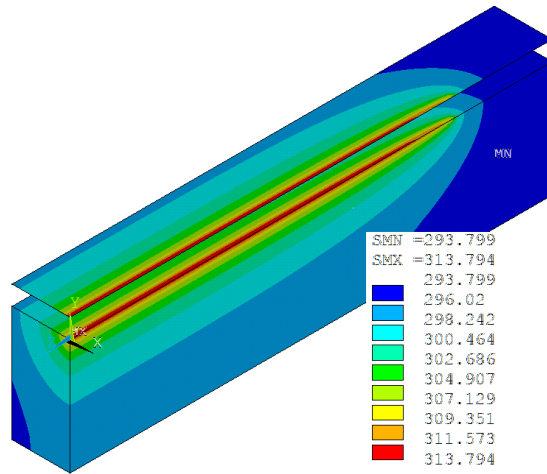
## Multilayer

3. Water cooling
4. LN cooling

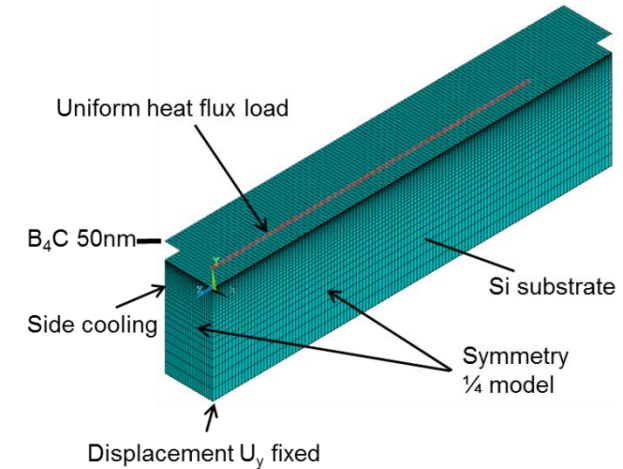


# Thermal stress prediction in mirror and multilayer coatings

## Single layer white beam mirror – water cooling

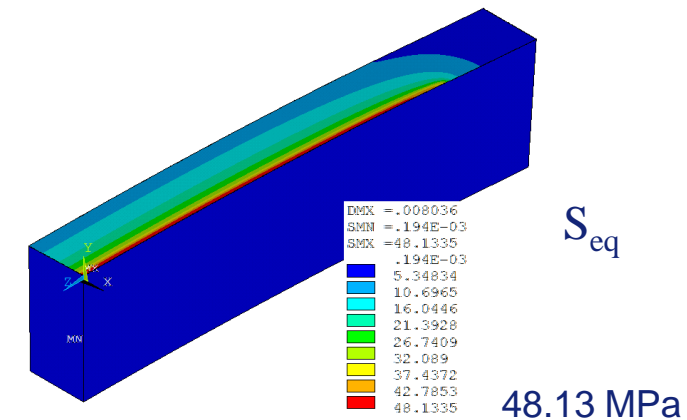
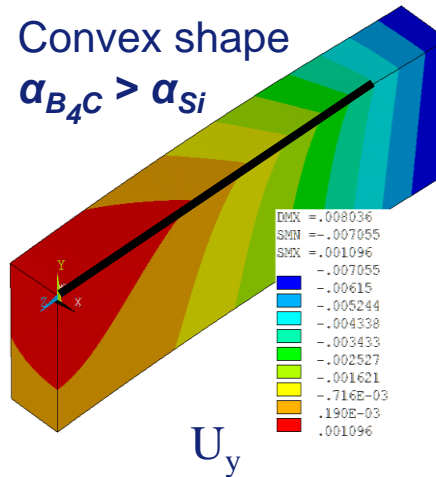


Coating:  $B_4C$  50 nm  
Si Substrate:  $60 \times 60 \times 500$  mm<sup>3</sup>  
Slits (H×V):  $4 \times 2$  mm<sup>2</sup>  
Power density:  $P_a = 100$  W/mm<sup>2</sup>  
Grazing angle:  $\alpha_{inc} = 5$  mrad  
Footprint length:  $2/\sin(\alpha_{inc}) = 400$  mm  
Water cooling:  
 $H_{cv} = 0.005$  W/mm<sup>2</sup>/K,  $T_{cool} = 293$  K



Temperature difference  
within the coating layer  
FEA:  $\Delta T = 0.553$  mK

Analysis using 1D  
conduction: 0.595 mK

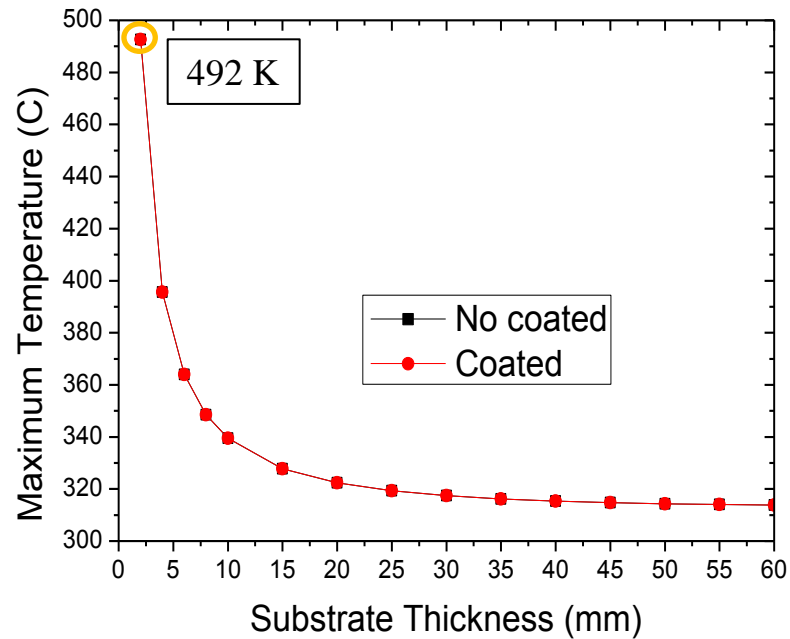


**Compressive stress in the coating layer**  
Negligible stress in the substrate

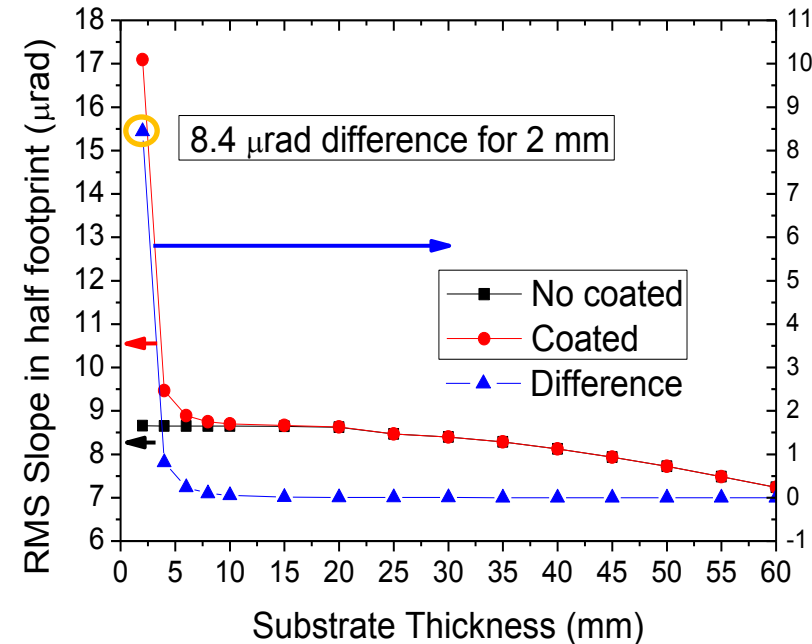
# Thermal stress prediction in mirror and multilayer coatings

## Single layer white beam mirror – water cooling

- One interesting issue: substrate becomes thinner



$$T_{\max} \sim t_{\text{substrate}}$$



$$\text{Slope}_{\text{RMS}} \sim t_{\text{substrate}}$$

- For  $t_{\text{substrate}} = 2 \text{ mm}$ , slope error change due to coating is 8.4 μrad.

# Thermal stress prediction in mirror and multilayer coatings

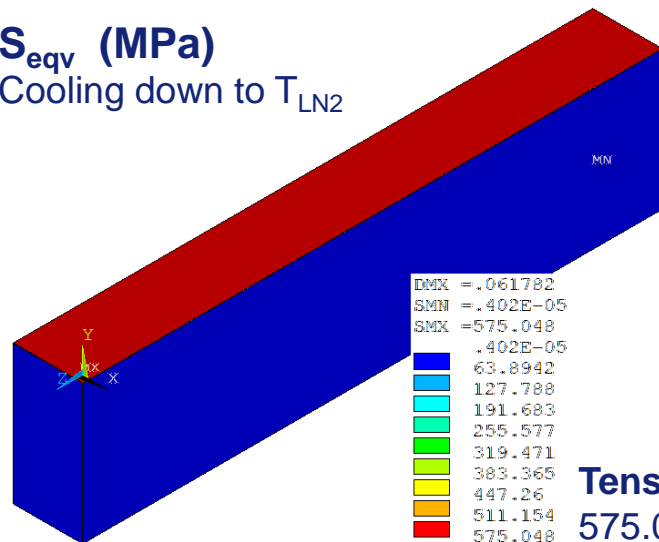
## Single layer white beam mirror – liquid-nitrogen (LN2) cooling

$$h_{cv}=5000 \text{ W/m}^2/\text{K}$$

$$T_{cool}=80 \text{ K}$$

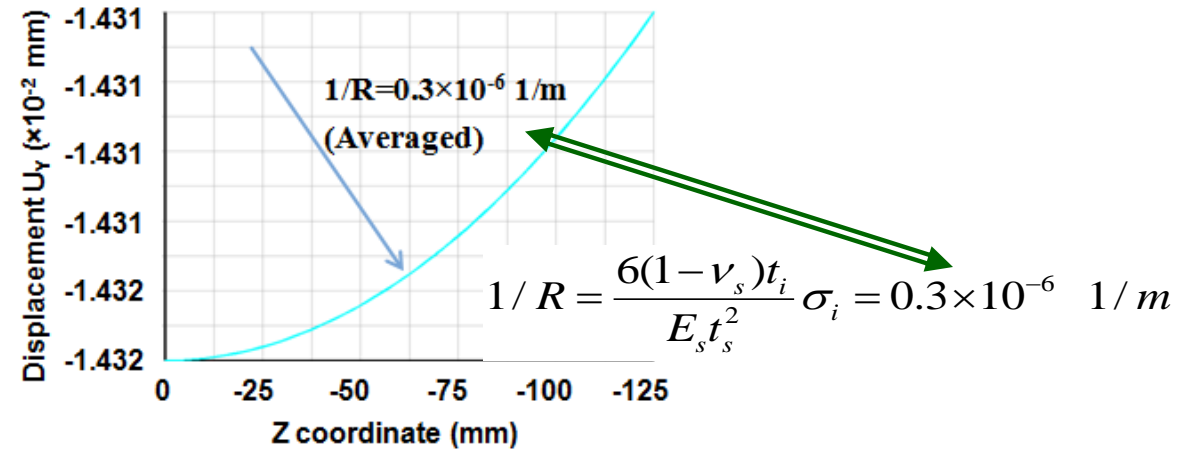
$S_{eqv}$  (MPa)

Cooling down to  $T_{LN2}$

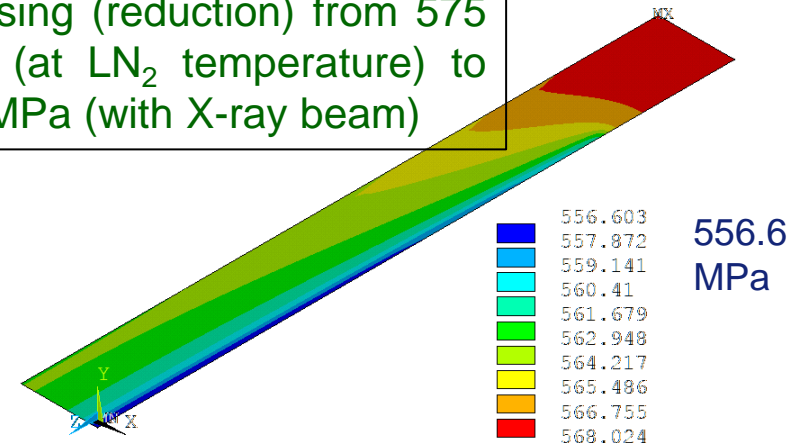


**Tensile stress**  
575.048 MPa

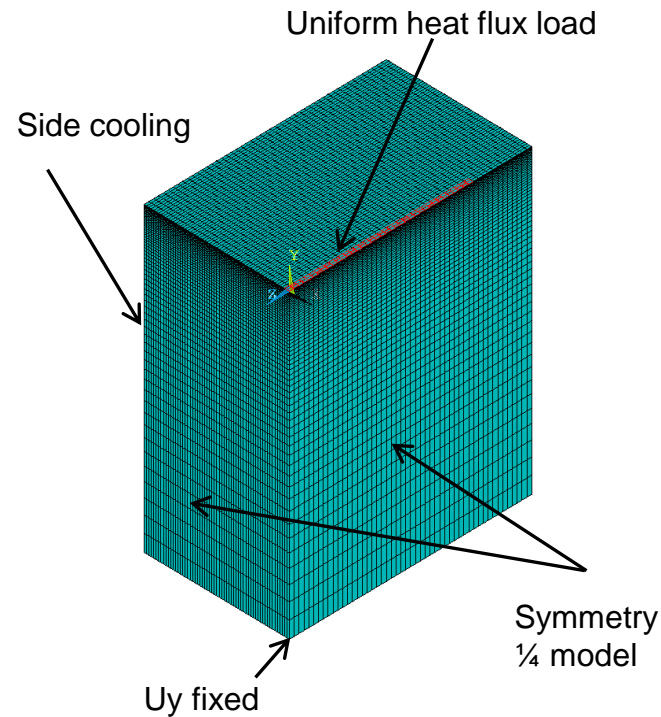
$$\sigma_i \approx \frac{E_i}{1-\nu_i} (\alpha_s - \alpha_i) \Delta T = 575.1 \text{ MPa}$$



Heat load leads to stress releasing (reduction) from 575 MPa (at  $LN_2$  temperature) to 557 MPa (with X-ray beam)



## Multilayer white beam monochromator – water cooling



FE model (1/4) and boundary conditions

Coating:  $[\text{Pd/B}_4\text{C}]_{80}$  2 nm

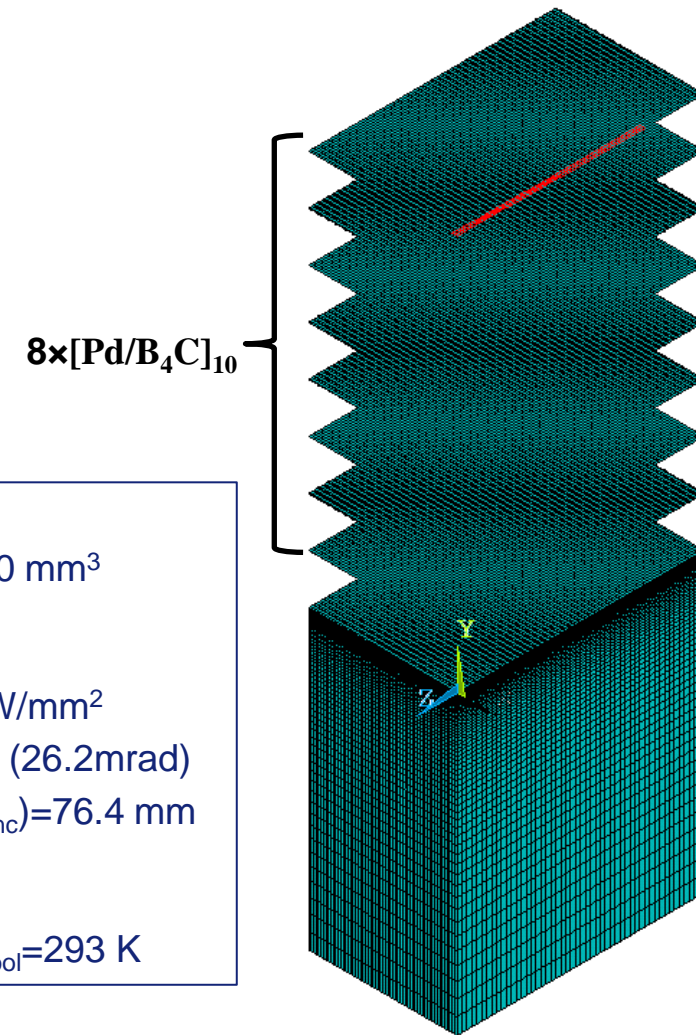
- Si Substrate:  $60 \times 60 \times 100 \text{ mm}^3$

Slits (H×V):  $2 \times 2 \text{ mm}^2$

- Power density:  $P_a = 200 \text{ W/mm}^2$
- Grazing angle:  $\alpha_{\text{inc}} = 1.5^\circ$  (26.2 mrad)
- Footprint length:  $2/\sin(\alpha_{\text{inc}}) = 76.4 \text{ mm}$

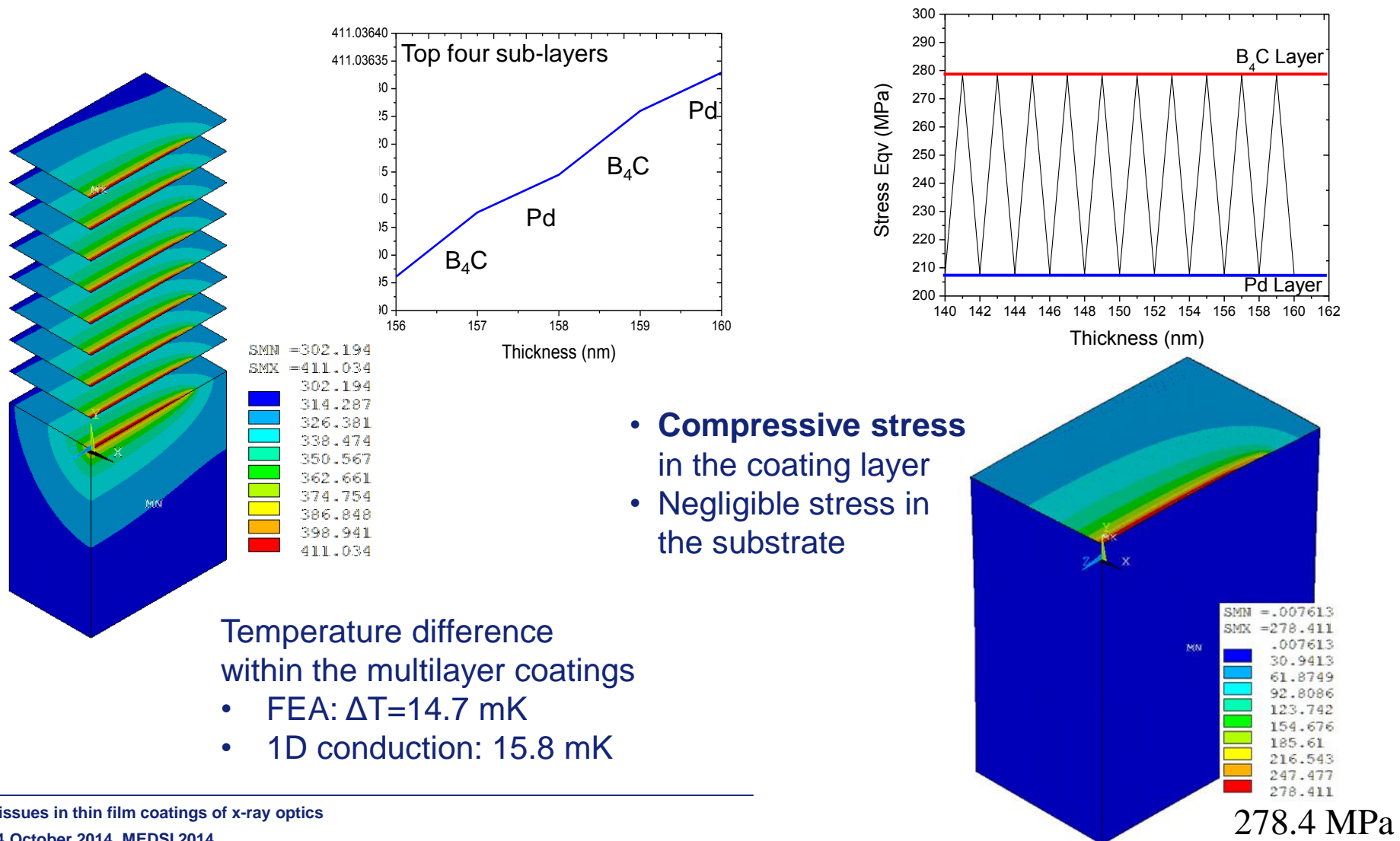
Water cooling:

- $H_{\text{cv}} = 0.005 \text{ W/mm}^2/\text{K}$ ,  $T_{\text{cool}} = 293 \text{ K}$



# Thermal stress prediction in mirror and multilayer coatings

## Multilayer white beam monochromator – water cooling

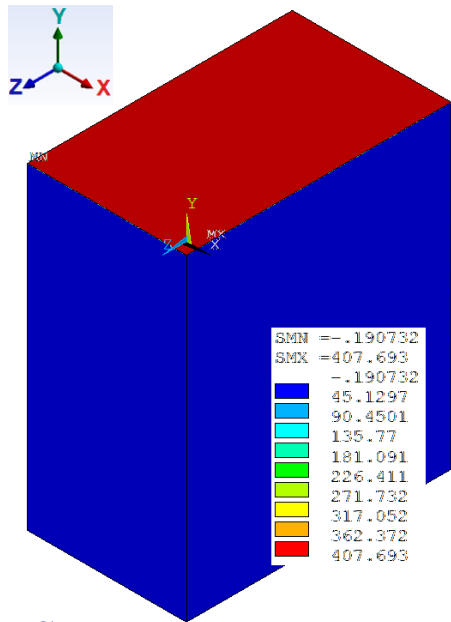


# Thermal stress prediction in mirror and multilayer coatings

## Multilayer white beam monochromator – LN2 cooling

Uniform temperature

$T_{\text{room}} \rightarrow T_{\text{LN2}}$



Analytical estimation for layer stress ( $S_x$ ,  $S_z$ ):

$$\sigma_i = \frac{E_i}{1 - \nu_i} (\alpha_s - \alpha_i) \Delta T$$

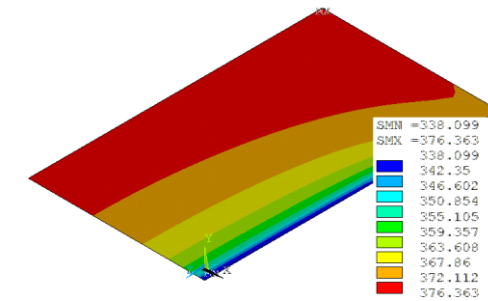
*Difference between the sub-layer and substrate i:  $B_4C$  or Pd*

**Tensile stress**  
408 MPa

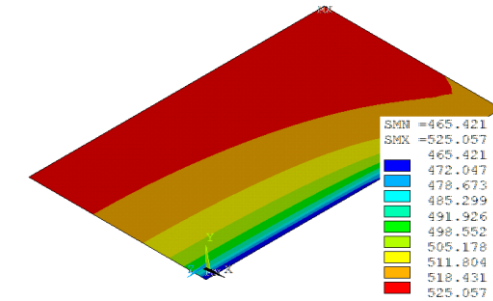
$S_{eq}$

Stress (MPa)	Pd sub-layer	$B_4C$ sub-layer
analytical: $T_{\text{room}} \rightarrow T_{\text{LN2}}$	407.7	575.1
FEA: $T_{\text{room}} \rightarrow T_{\text{LN2}}$	407.7	575.0
FEA: with X-ray beam	338.1	465.4

With X-ray beam (800 W)



$S_{eq}$  in Pd sub-layer



$S_{eq}$  in  $B_4C$  sub-layer

110 MPa stress releasing  
with X-ray beam

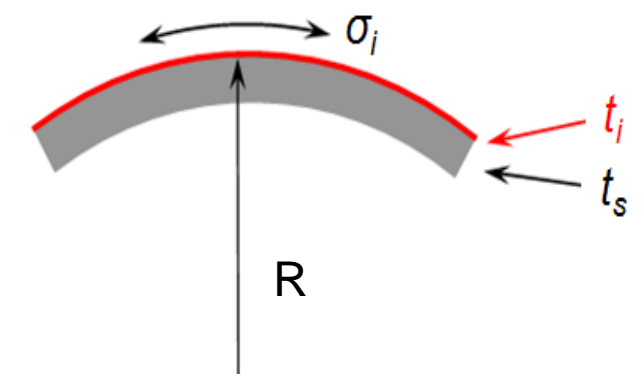


# Measurement: thermal deformation properties of thin coating film

- Mechanical properties of thin film are **different** from bulk material
- Limited data in literature for thin film
- Experimental measurements

## Experimental principle

- uniform temperature change  $\Delta T$   
→ curvature change  $\Delta(1/R)$
- It can be shown that


$$\text{define } K = \underbrace{\frac{E_i}{1-\nu_i}(\alpha_i - \alpha_s)}_{\text{Thermal deformation properties}} = \underbrace{\left(\Delta \frac{1}{r} / \Delta T\right)}_{\text{Measurement results}} / \underbrace{\left[\frac{6(1-\nu_s)t_i}{E_s t_s^2}\right]}_{\text{Known parameters}}$$

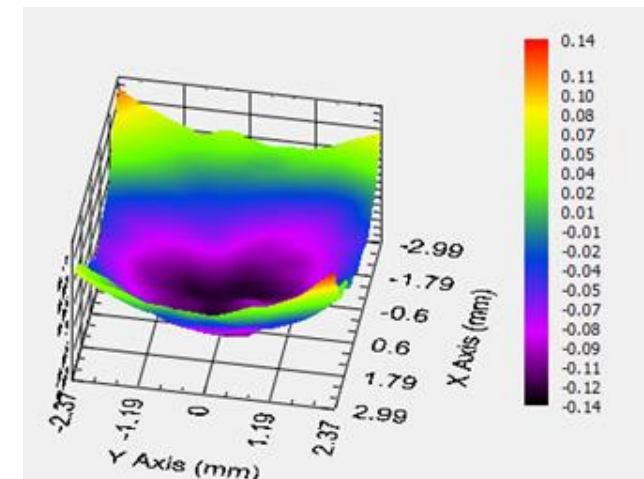
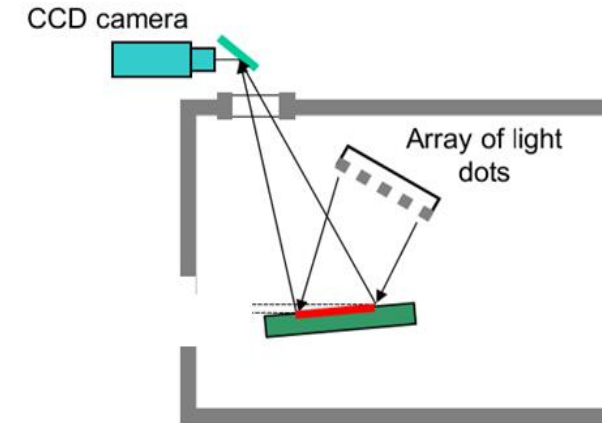
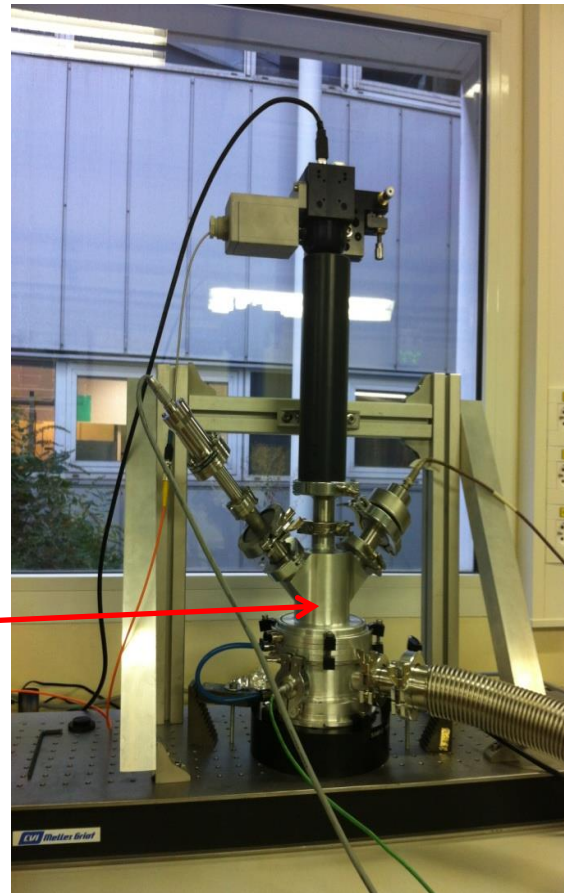
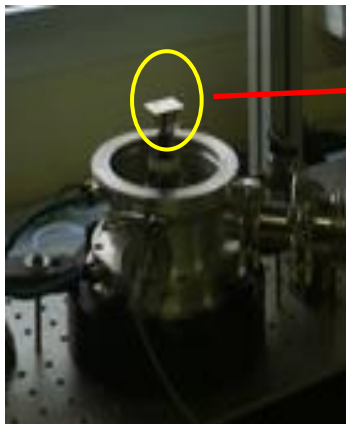
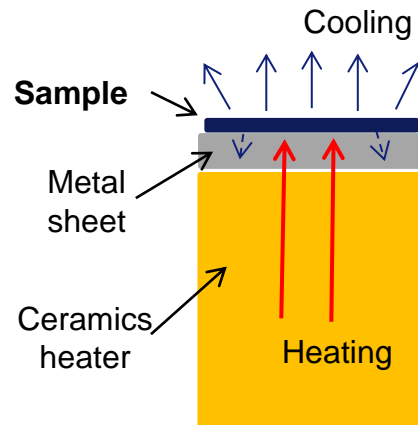
- For multilayer structure 
$$K = \frac{t_1 \cdot K_1 + t_2 \cdot K_2}{t_1 + t_2}$$

- $K$  is a combination of parameters  $E$ ,  $\alpha$ ,  $\nu$
- The physics meaning of the composite parameter: 
$$\sigma_i = K \cdot \Delta T$$



# Measurement: thermal deformation properties of thin coating film

## ➤ Experiment setup



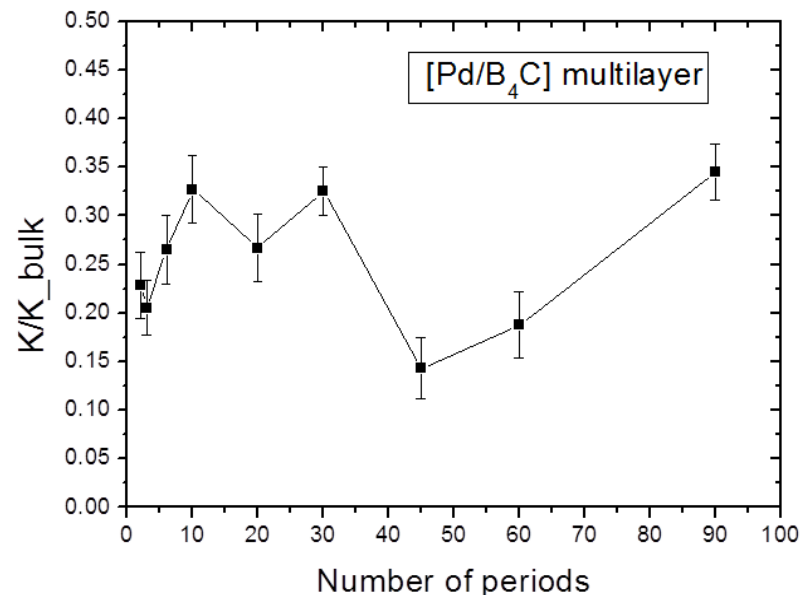
# Measurement: thermal deformation properties of thin coating film

## ➤ Experiment results – Single layer coatings (substrate Si 200 $\mu$ m)

Layer	B <sub>4</sub> C 50 nm	B <sub>4</sub> C 20 nm	B <sub>4</sub> C 10 nm	Pd 200 nm	Pd 100 nm	Pd 50 nm	Cr 200 nm	Cr 100 nm	Cr 50 nm
K (MPa/°C)	<b>0.193</b>	<b>0.874</b>	<b>0.918</b>	<b>1.322</b>	<b>1.166</b>	<b>0.749</b>	<b>0.968</b>	<b>0.509</b>	<b>0.514</b>
K_bulk	<b>1.93</b>			<b>1.63</b>			<b>1.27</b>		

## ➤ Experiment results – [Pd/B<sub>4</sub>C] Multilayer coatings (substrate Si 200 $\mu$ m)

Total thicknesses of the coatings are maintained at 180nm when varying the number of periods



In all the cases, the composite parameter K of the thin coating film is **significantly smaller (1/3)** than one of the bulk material

→ Thermal stress is effectively lower

- **FEA of multilayer optics allows to study the thin coating layers**
- **Coating layers on the Mirror or multilayer optics under white beam:**
  - Negligible influence on temperature, deformation of the optics
  - Negligible influence on the stress of the substrate
- **Large thermal stress in the coating layer due to thermal mismatch between layer(s) and substrate**
$$\sigma_i = \frac{E_i}{1-\nu_i} (\alpha_s - \alpha_i) \Delta T$$
- **Water cooled Mirror or multilayer optics under X-ray beam**
  - Mostly negligible, compressive stress when using silicon as substrate (if  $\alpha_i > \alpha_{Si}$ )
- **LN2 cooled Mirror or multilayer optics with Si-substrate**
  - Cooling down from  $T_{\text{room}}$  to  $T_{\text{LN2}}$  → large tensile stress (most critical case)
  - Additional X-ray beam power → additional compressive stress → globally stress released in the coating layers
- **Thin-coating material properties:**
$$K = \frac{E_i}{1-\nu_i} (\alpha_i - \alpha_s)$$
  - Smaller composite parameter K than bulk material
  - Smaller stress in coating layers than expected with bulk material properties
- **Intrinsic stress from deposition (0.5~1.0 GPa compressive)**
  - LN2 cooling induced tensile stress should offset this Intrinsic stress from deposition